# PHASE EQUILIBRIA IN THE SYSTEM NH<sub>4</sub>Al(SO<sub>4</sub>)<sub>2</sub>–H<sub>2</sub>SO<sub>4</sub>–H<sub>2</sub>O

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#### Abstract

Equilibrium solubility curves of the ammonium aluminium sulphate in aqueous solutions of sulphuric acid have been calculated using checked literature data and our own measurements. The concentration of sulphuric acid ranged from 0 to 23 mass%, temperature range between 20 and 60°C has been extrapolated up to 75°C by means of a thermodynamically based correlation method. The solubility correlation as well as the hydration analysis implied a possible destructuralization of solutions at higher acid concentrations.

Keywords: ammonium aluminium sulphate, solubility, sulphuric acid

#### Introduction

This paper is linked with a communication [1] dealing with a treatment of solutions from chemical extraction of uranium ores. The aim of this paper is to evaluate our experimental data and available literature data of the system  $NH_4Al(SO_4)_2-H_2SO_4-H_2O$  and in this way to obtain an insight into possible structure changes in the solution.

#### Theoretical

For a phase equilibrium of the solid (') and liquid (") phase follows [2]

$$\log \frac{m_{\rm i}}{m_{\rm 0i} y_{\rm i}} = \log \frac{\gamma_{\rm i}' \gamma_{\rm 0i}'}{\gamma_{\rm i}''} \tag{1}$$

where  $m_i$  is the molality of the *i*-th component in the solution,  $m_{0i}$  is the molality (solubility) of the pure *i*-th component in water under identical conditions (temperature, pressure),  $y_i$  is mole fraction of the *i*-th component in solid phase and  $\gamma_i$  are the corresponding activity coefficients. Introducing notations for the relative molality

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$$X_{i} = \frac{m_{i}}{m_{0i}}$$
(2)

and for the relative activity coefficient of *i*-th component in the liquid phase

$$\xi_{i} = \frac{\gamma_{i}''}{\gamma_{0i}''} \tag{3}$$

we obtain

$$\log \frac{x_i}{y_i} = -\log \frac{\xi_i}{\gamma_i} = \phi_i$$
(4)

This relationship can be modified for a three-component system:

$$\log \frac{x_1 y_2}{x_2 y_1} = \varphi_1 - \varphi_2 \tag{5}$$

or

$$K = \frac{y_2 x_1}{y_1 x_2} \approx \frac{p'_2 p''_1}{p'_1 p''_2}$$
(6)

where *K* is a distribution coefficient.

For dissociated substances possessing a common anion, Eq. (4) converts into

$$\frac{1}{\nu_{1}}\log\left[\left(X_{1}+X_{2}\frac{m_{20}}{m_{10}}\right)^{\nu_{1-}}X_{1}^{\nu_{1+}}\right]-\log y_{1}=\phi_{1}$$
(7)

holding for the solubility of the component 1, and the  $\phi_{\scriptscriptstyle 1}$  can be approximated by the expansion

$$\varphi_1 = Q_{12}m_2 + Q_{122}m_2^2 + \dots \tag{8}$$

Solution of this equation is relatively complicated but it can be simplified [2] for the case where no solid solutions are formed

$$\frac{1}{\nu_{1}}\log\left[\left(X_{1}+X_{2}\frac{m_{20}}{m_{10}}\right)^{\nu_{1-}}X_{i}^{\nu_{1+}}\right]=\phi_{1}$$
(9)

A suitable shape of this equation can be obtained

$$\frac{1}{b_1 + h_1} \log \left[ X_1^{b_1} \left( X_1 + \frac{h_2}{h_1} X_2 \right)^{h_1} \right] = Q_{12} m_2 + Q_{122} m_2^2 + Q_{1222} m_2^3$$
(10)

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where  $b_1$  is the number of cations in the component 1 and  $h_1$  and  $h_2$  the number of common anions in components 1 and 2, respectively.  $X_i$  is the relative molality of the *i*-th component related to its solubility in pure water.

### Data and their treatment

Solubility data of the ammonium aluminium sulphate in aqueous solutions of the sulphuric acid have been published in the paper [3] for temperature 30°C, in the paper [4] for temperatures 20 and 30°C. These data have been complemented by our measurements at 25, 30, 40, 50 and 60°C and by several measurements at higher temperatures.

 Table 1 Solubility data in the system ammonium aluminium sulphate (AAS)–sulphuric acid (SA)–H2O

T/0C	p/mass%					а		G
1/°C	$H_2SO_4$	AAS <sub>anh</sub>	AAS <sub>hyd</sub>	H <sub>2</sub> O <sub>tot</sub>	$H_2O_{free}$	AAS <sub>anh</sub>	Whyd	Source
20	0	5.28	10.10	94.72	89.90	5.57	0.112	2
	1.05	5.56	10.63	93.39	88.32	5.95	0.120	
	5.5	6.03	11.53	88.47	82.97	6.82	0.139	
	7.2	6.03	11.53	86.77	81.27	6.95	0.142	
	9.2	5.97	11.41	84.83	79.39	7.04	0.144	
	10.1	5.91	11.30	83.99	78.60	7.04	0.144	
	13	5.63	10.76	81.37	76.24	6.92	0.141	
	17	5.22	9.98	77.78	73.02	6.71	0.137	
	22.8	4.47	8.57	72.72	68.63	6.16	0.125	
25	0	5.85	11.19	94.15	88.81	6.21	0.126	this work
	1.25	6.05	11.57	92.7	87.18	6.53	0.133	
	2	6.4	12.24	91.6	85.76	6.99	0.143	this work
	2.6	6.6	12.62	90.8	84.78	7.27	0.149	
	4	6.75	12.91	89.25	83.09	7.56	0.155	
	5.2	6.9	13.19	87.9	81.61	7.85	0.162	
	6.6	7	13.38	86.4	80.02	8.10	0.167	
	7.05	7	13.38	85.95	79.57	8.14	0.168	
	8.35	6.95	13.29	84.7	78.36	8.21	0.170	
	9.8	6.8	13.00	83.4	77.20	8.15	0.168	
	10.5	6.7	12.81	82.8	76.69	8.09	0.167	
	13	6.1	11.66	80.9	75.34	7.54	0.155	
	14.3	6.05	11.57	79.65	74.13	7.60	0.156	
	16	5.8	11.09	78.2	72.91	7.42	0.152	

T/°C			p/mass%	а	10	C		
	$H_2SO_4$	AAS <sub>anh</sub>	AAS <sub>hyd</sub>	$H_2O_{tot}$	H <sub>2</sub> O <sub>free</sub>	AAS <sub>anh</sub>	Whyd	Source
25	17.85	5.45	10.42	76.7	71.73	7.11	0.145	
	19.6	5	9.56	75.4	70.84	6.63	0.135	
	20.55	4.85	9.27	74.6	70.18	6.50	0.132	
	21.85	4.65	8.89	73.5	69.26	6.33	0.128	
30	0	7.15	13.67	92.85	86.33	7.70	0.158	2
	2	7.77	14.86	90.23	83.14	8.61	0.179	
	8.1	8.11	15.51	83.79	76.39	9.68	0.203	
	10	7.89	15.09	82.11	74.91	9.61	0.201	
	11.8	7.77	14.86	80.43	73.34	9.66	0.203	
	15.7	7.21	13.79	77.09	70.51	9.35	0.195	
	15.7	7.33	14.01	76.97	70.29	9.52	0.199	
	17	7.12	13.61	75.88	69.39	9.38	0.196	
	17	7.43	14.21	75.57	68.79	9.83	0.207	
	18.6	6.84	13.08	74.56	68.32	9.17	0.191	
	20.5	6.62	12.66	72.88	66.84	9.08	0.189	
30	0	7.08	13.54	92.92	86.46	7.62	0.157	3
	2.1	7.69	14.71	90.21	83.19	8.53	0.177	
	4.12	7.89	15.08	87.99	80.80	8.96	0.187	
	6.06	8.11	15.51	85.83	78.43	9.45	0.198	
	7.96	8.09	15.46	83.95	76.58	9.63	0.202	
	9.85	7.90	15.11	82.25	75.04	9.61	0.201	
	11.69	7.76	14.84	80.55	73.47	9.64	0.202	
	13.52	7.55	14.43	78.93	72.05	9.56	0.200	3
	15.36	7.20	13.77	77.44	70.87	9.30	0.194	
	15.35	7.23	13.83	77.42	70.82	9.34	0.195	
	17.07	7.14	13.66	75.79	69.27	9.43	0.197	
	17.19	6.84	13.07	75.97	69.74	9.00	0.187	
	18.93	6.66	12.73	74.41	68.34	8.95	0.186	
	18.89	6.78	12.97	74.33	68.14	9.13	0.190	
	20.7	6.36	12.16	72.94	67.14	8.72	0.181	
	22.4	6.16	11.78	71.44	65.82	8.62	0.179	
30	0	7	13.38	93	86.62	7.53	0.155	this worl
	1.25	7.2	13.76	91.55	84.98	7.86	0.162	
	2.3	7.45	14.24	90.25	83.46	8.25	0.171	

Tabl	le 1	Continued	1

TIOC	p/mass%					a		G
<i>1/1</i> C	$H_2SO_4$	AAS <sub>anh</sub>	$AAS_{hyd}$	$\mathrm{H_2O_{tot}}$	$H_2O_{free}$	AAS <sub>anh</sub>	Whyd	Source
	3.55	7.6	14.53	88.85	81.92	8.55	0.177	
	5.55	7.85	15.00	86.6	79.44	9.06	0.189	
	6	7.9	15.10	86.1	78.90	9.18	0.191	
	7.15	7.85	15.01	85	77.84	9.24	0.193	
	8.3	7.85	15.01	83.85	76.69	9.36	0.196	
	9.5	7.75	14.82	82.75	75.68	9.37	0.196	
	10.4	7.7	14.72	81.9	74.88	9.40	0.197	
	11.9	7.55	14.44	80.55	73.66	9.37	0.196	
	14.35	7.25	13.86	78.4	71.79	9.25	0.193	
	16.7	6.9	13.19	76.4	70.11	9.03	0.188	
	18.4	6.6	12.62	75	68.98	8.80	0.183	
	19.8	6.35	12.14	73.85	68.06	8.60	0.178	
	21.05	6.1	11.66	72.85	67.29	8.37	0.173	
40	0	9.6	18.35	90.4	81.64	10.62	0.225	this work
	1.2	9.75	18.64	89.05	80.16	10.95	0.233	
	2.1	9.9	18.93	88	78.97	11.25	0.240	
	3.05	10.05	19.22	86.9	77.73	11.57	0.247	
	5.1	10.35	19.73	84.55	75.11	12.24	0.263	
	7.2	10.45	19.98	82.35	72.82	12.69	0.274	
	9.08	10.42	19.92	80.5	71.00	12.94	0.281	
	10.8	10.3	19.69	78.9	69.51	13.05	0.283	
	12	10.2	19.50	77.8	68.50	13.11	0.285	
	14.35	9.95	19.02	75.7	66.63	13.14	0.286	
	15.55	9.8	18.74	74.65	65.71	13.13	0.285	
	17.95	9.45	18.07	72.6	63.98	13.02	0.282	
	19.7	9.25	17.69	71.05	62.61	13.02	0.282	
50	0	13.25	25.33	86.75	74.67	15.27	0.339	this work
	1.2	13.05	24.95	85.75	73.85	15.22	0.338	
	2.45	13.15	25.14	84.4	72.41	15.58	0.347	
	3.6	13.25	25.3	83.15	71.07	15.94	0.356	
	5.3	13.4	25.62	81.3	69.08	16.48	0.371	
	6.15	13.5	25.8	80.35	68.04	16.80	0.379	
	7.6	13.55	25.91	78.85	66.49	17.18	0.390	

Table 1 Continued

T/0C	p/mass%					а	141-	Sauraa
17 C	$H_2SO_4$	AAS <sub>anh</sub>	$AAS_{hyd}$	$H_2O_{tot}$	$H_2O_{free}$	AAS <sub>anh</sub>	Whyd	Source
50	9.85	13.5	25.81	76.65	64.34	17.61	0.401	
	11.05	13.45	25.72	75.5	63.23	17.81	0.407	
	13	13.4	25.62	73.6	61.38	18.21	0.417	
	14.8	13.2	25.23	72	59.96	18.33	0.421	
	15.95	13.1	25.04	70.95	59.00	18.46	0.425	
	17.1	13.1	25.04	69.8	57.85	18.77	0.433	
	18.45	12.95	24.76	68.6	56.79	18.88	0.436	
58	1.6	17.2						this work
58.5	0	17.17						
60	0	17.17	32.82	82.83	67.17	20.73	0.489	this work
	1.9	17.15	32.79	80.95	65.31	21.19	0.502	
	4.4	17.1	32.70	78.5	62.90	21.78	0.520	
	5.95	17.2	32.89	76.85	61.16	22.38	0.538	
	7.2	17.25	32.98	75.55	59.82	22.83	0.551	
	9.55	17.4	33.27	73.05	57.18	23.82	0.582	
	11.95	17.5	33.46	70.55	54.59	24.81	0.613	
	13.45	17.55	33.56	69	52.99	25.43	0.633	
	14.7	17.5	33.46	67.8	51.84	25.81	0.645	
	16	17.35	33.17	66.65	50.83	26.03	0.653	
62.5	1.0	21.0						this work
67.7	2.5	24.5						
68.3	5.0	24.0						
71.7	3.0	26.0						
72.0	7.0	69.0						this work
72.0	7.0	23.0						
73.5	1.0	26.0						

Table 1 Continued

The ammonium aluminium sulphate used for our measurements was produced in Spolchemie for the production of synthetic corundum single crystals, several times recrystallized from demineralized water and its purity checked by atomic absorption (Varian AA-30) and X-ray spectrography (Philips PV-1404). Its purity has been found as 99.966 mass%. The sulphuric acid used was reagent grade product by Spolchemie. The conductivity of the demineralized water was about 5  $\mu$ S. Isothermal data as well as the literature data were obtained using an analytical method, our measurements were based on a polythermal method (components altogether 100 g weighted into a closed bottle and heated with the rate 1 K h<sup>-1</sup> until the last crystals dis-



**Fig. 1** Polythermic measurement of the solubility in the system: ammonium aluminium sulphate (AAS)–sulphuric acid (SA)–water. Number at the points denote the measured temperature of solubility, the curves have been calculated by the correlation method [5] using constants from Table 2

appeared); polytherms were obtained by interpolation of close lying data. Their accuracy is lower at higher temperatures, as can be seen from Fig. 1. Literature data as well as the results of the analytical method of our measurement show clearly that in the investigated concentration range the ammonium aluminium sulphate dodeca-hydrate is the sole existing solid phase. All data are summarized in Table 1.

T/°C	$Q_{12}$	$Q_{122}$	Q <sub>1222</sub>	Source	
20	0.6419 <sub>676</sub>	-0.3811 <sub>565</sub>	0.0726 <sub>740</sub>	3	
25	$0.5770_{921}$	$-0.3082_{100}$	0.0554983	this work	
30	$0.5254_{287}$	$-0.2902_{007}$	0.0567978	3	
	$0.4898_{424}$	$-0.2410_{185}$	$0.0418_{761}$	2	
	$0.4625_{706}$	$-0.2245_{395}$	$0.0397_{830}$	this work	
40	0.3358683	$-0.1309_{507}$	0.0206475	this work	
50	0.1837431	$-0.0255_{506}$	0	this work	
55	0.170	-0.0150	0	interpolation	
60	0.1545808	$-0.0195_{539}$	0	this work	
65	0.110	-0.010	0	extrapolation	
70	0.080	-0.0018	0	extrapolation	
75	0.070	-0.0010	0	extrapolation	

**Table 2** Interaction constants Q of the system ammonium aluminium sulphate–sulphuricacid–water

The values of the constants Q evaluated using the method described in detail and checked on many inorganic systems in the book [2] are summarized Table 2 and shown in Fig. 2.

Using known values Q we can recalculate the smoothed solubilities of component 1 for any given concentration of the component 2 using Eq. (10), (Fig. 2).

Hydration analysis [6, 7], based on Eq. (11), can provide some information on the intrinsic structure of the solution.

$$P = \frac{1 - w_1 - w_2 - w_{0 \text{ vol}}}{M_0 (n_1 + n_2)} \tag{11}$$

From this equation, values of the hydration parameter P and of the ratio  $P/x_2$  shown in Fig. 3 and given in Table 3 for three values chosen for each system, were obtained.

<i>T</i> /°C	Source	%H <sub>2</sub> SO <sub>4</sub>	Р	$P/x_2$
20	3	1.05	-0.182	-89.02
		9.20	-1.11	-57.09
		22.8	-1.84	-33.99
25	this work	1.25	-0.171	-70.41
		9.80	-1.14	-54.40
		20.55	-1.51	-31.43
30	3	2.00	-0.28	-68.95
		10.00	-0.96	-44.10
		20.50	-1.48	-30.40
	2	2.10	-0.29	-67.95
		9.85	-0.97	-45.32
		20.70	-1.46	-29.61
	this work	1.25	-0.15	-59.58
		9.50	-0.93	-45.58
		21.05	-1.44	-28.85
40	this work	1.20	-0.10	-42.48
		10.80	-0.82	-33.88
		19.70	-1.24	-25.90
50	this work	1.20	-0.05	-19.59
		9.85	-0.56	-24.68
		18.45	-0.98	-21.06
60	this work	1.90	-0.09	-20.51
		9.56	-0.46	-20.09
		16.00	-0.78	-18.75

Table 3 Selected results of the hydration analysis



Fig. 2 Solubility in the system: ammonium aluminium sulphate (AAS)–sulphuric acid (SA)–water. Individual curves have been calculated from Eq. (9)

#### Discussion

Literature data used for the treatment have been limited up to sulphuric acid concentration below 23%. Results with higher acid concentrations couldn't be correlated with sufficient accuracy using given Q constants. This may be explained by a more complicated interactions in the solution and probably also by a lower data precision [3]. It has been shown [4] as well that the character of the solubility at acid concentrations above 30% is changed: the solubility up to 8% H<sub>2</sub>SO<sub>4</sub> slightly rises, between 8 and 32% H<sub>2</sub>SO<sub>4</sub> diminishes, passes through a minimum and at higher acid concentrations rises again.

It can be seen from Table 2 that the absolute values of the interaction constants Q decrease with rising the temperature. This is not unexpected, as the behaviour of the solution approaches ideality with higher temperatures. Up to 50°C three constants are required for the correlation, at higher temperatures  $Q_{122}=0$ , and just two constants are sufficient. The constants for temperatures above 60°C were obtained by a graphical extrapolation. At the same time, no new interactions can be expected at slightly higher temperatures so that the extrapolation seems to be safe in this case; its acceptance is checked by polythermal data shown in Fig. 1.

It can be concluded from the interaction constants [7]  $Q_{12}>0$  a  $Q_{122}<0$  that in particular at higher acid concentrations occurs some destructuralization of the solution. This corroborates as well the values of the hydration parameter P<0 approaching a constant value and slightly rising values of  $P/x_2<0$  at lower temperatures. On the other hand we can conclude from almost constant values of  $x_0/s$  that the sulphuric acid up to 20% doesn't remove water from the hydration sphere of the alum.



**Fig. 3** Hydration analysis of the system: ammonium aluminium sulphate (AAS)–sulphuric acid (SA)–water. Corresponding temperatures are given in the right upper corner. Plotted are relative values related to the rounded maxims

The value of the hydration parameters P and  $P/x_2$  is extremely sensitive [6] to the quality of experimental data. The smooth curves on Fig. 3 thus demonstrate that the data obtained are sufficiently reliable.

## Notations

a	concentration (g/100 g $H_2O$ )
$b_1$	number of different cations in component 1
$h_1$	number of common anions in component 1
K	distribution coefficient
$M_{\rm anh}, M_{\rm i}$	molecular mass of anhydrous substance (g mol <sup>-1</sup> )
$M_0$	molecular mass of water $(g mol^{-1})$
$m_{i}$	molality of the <i>i</i> -th component (mol kg <sup><math>-1</math></sup> H <sub>2</sub> O)
$m_{0i}$	molality of the <i>i</i> -th component in pure water (mol kg <sup><math>-1</math></sup> H <sub>2</sub> O)
n <sub>i</sub>	number of moles in 100 cm <sup>3</sup> $H_2O$ mol/100 cm <sup>3</sup> $H_2O$
Р	hydration parameter
$p, p_i$	concentration (mass%)
$Q_{1i}, Q_{122}$	interaction constants
S	number of components
Т	temperature (°C)
W <sub>i</sub>	concentration (kg kg <sup>-1</sup> )
$W_{0vol}$	concentration of free water (kg kg <sup>-1</sup> )
X	relative molality
x <sub>i</sub>	mole fraction in liquid
$x_0$	amount of water outside the hydration sphere (kg/kg)
${\cal Y}_{ m i}$	mole fraction in solid
$\gamma_{i}$	activity coefficient
$\boldsymbol{\phi}_{i}$	expansion function
$\nu_{i}$	number of ions
ξ <sub>i</sub>	relative activity coefficient
Subscripts:	
anh	anhydrous
free	free water
hyd	hydrate
tot	total

\* \* \*

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